

1521/203
1601/203
1602/203
MATHEMATICS II
June/July 2021
Time: 3 hours



THE KENYA NATIONAL EXAMINATIONS COUNCIL

CRAFT CERTIFICATE IN ELECTRICAL AND ELECTRONIC TECHNOLOGY
(POWER OPTION)
(TELECOMMUNICATION OPTION)
MODULE II

MATHEMATICS II

3 hours

INSTRUCTIONS TO CANDIDATES

You should have the following for this examination:

Answer booklet;

Mathematical tables/calculator;

Answer any FIVE of the EIGHT questions in the answer booklet provided.

All questions carry equal marks.

All necessary working must be clearly shown.

Maximum marks for each part of a question are as indicated.

Candidates should answer all questions in English.

This paper consists of 5 printed pages.

Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.

1. (a) Three currents I_1 , I_2 and I_3 in amperes in an electric circuit satisfy the simultaneous equations

$$6I_1 + 3I_2 + 2I_3 = 15$$

$$-3I_1 + 2I_2 + 6I_3 = 10$$

$$2I_1 - 6I_2 + 3I_3 = 19$$

Use elimination to solve the equations.

(11 marks)

- (b) Solve the equation

$$2^{2x} + 14(2^x) + 45 = 0$$

giving the answer correct to three significant figures.

(9 marks)

2. (a) Given the function $\phi(x, y) = \frac{x^3}{y}$, determine:

(i) $\frac{\partial^2 \phi}{\partial x^2}$;

(ii) $\frac{\partial^2 \phi}{\partial y^2}$

(4 marks)

- (b) The dimensions of a solid cuboid are $x = 24$ cm, $y = 19$ cm and $z = 11$ cm. If x , y and z are increased by 0.1 cm, increased by 0.3 cm and decreased by 0.4 cm respectively, determine the change in its volume.

(7 marks)

- (c) Determine the stationary points of the function $f(x) = 2x^3 - 3x^2 - 36x + 7$ and classify them.

(9 marks)

3. (a) Given that $\cosh x = \frac{e^x + e^{-x}}{2}$ and $\sinh x = \frac{e^x - e^{-x}}{2}$, prove that

(i) $\cosh^2 x + \sinh^2 x = \cosh 2x$

(ii) $\cosh^2 x - \sinh^2 x = 1$

(8 marks)

- (b) Determine the values of constants M and N in the equation:

$$Me^x + Ne^{-x} = 10 \cosh x + 4 \sinh x$$

(4 marks)

- (c) Figure 1 shows three forces F_1 , F_2 and F_3 acting at a point O in a plane. Determine the:
- magnitude;
 - direction
- of the resultant force. (8 marks)

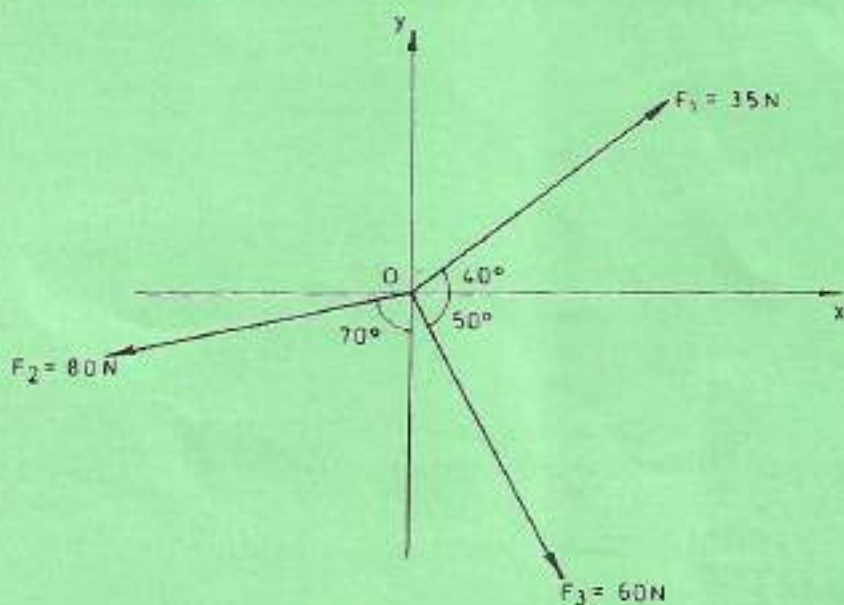


Fig.1

4. (a) A right angled triangle ABC has $\angle B = 90^\circ$, sides $AB = 40$ cm and $AC = 58$ cm. Determine the:

- angle $\angle A$;
- length of BC.

(6 marks)

- (b) Prove the identities;

- $\cos 4\theta + \cos 3\theta + \cos 2\theta = 2 \cos 3\theta (1 + \cos \theta)$
- $\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$

(8 marks)

- (c) Solve the equation:

$$\cos 2\theta + 4 \sin \theta - 3 = 0 \quad \text{for } 0 \leq \theta \leq 90^\circ.$$

(6 marks)

5. (a) Use substitution method to solve the simultaneous equations:

$$4x + y + 2z = 9$$

$$-x + y + 3z = -8$$

$$3x + 2y + z = 9$$

(10 marks)

- (b) A right angled triangle has sides $(2x+2)$ cm, $(2x+5)$ cm and $(x+7)$ cm. Determine the:

(i) value of x ;

(ii) length of each side.

(10 marks)

6. (a) Given the function $y = e^x \sin x$, show that:

$$\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 2y = 0$$

(5 marks)

- (b) Determine $\frac{dy}{dx}$ for the function given by:

(i) $y = \sin(x^2 + 2)$

(ii) the parametric equation $x = 16 \cos \theta$, $y = 9 \sin \theta$.

(8 marks)

- (c) Evaluate the integrals:

(i) $\int_1^2 x^3 dx$

(ii) $\int_0^{\frac{\pi}{2}} (\cos x + \sin x) dx$

(7 marks)

7. (a) Given the vectors $\underline{B} = 2\underline{i} + 3\underline{j} + \underline{k}$ and $\underline{I} = 4\underline{i} + \underline{j} - 2\underline{k}$, determine the:

(i) angle between the vectors;

(ii) unit vector perpendicular to both vectors.

(10 marks)

- (b) Given the vector field function $E = x^2yi + xyi - x^3zk$ and the scalar potential function $V = 4x^2z + 3yz^2$, determine at the point (1, 2, 1)

- (i) $\nabla \cdot E$
 (ii) $\nabla \times E$
 (iii) ∇V

(10 marks)

8. (a) Given the matrices

$$A = \begin{pmatrix} -4 & 3 & 5 \\ 2 & 6 & -1 \\ 8 & 9 & -6 \end{pmatrix} \text{ and } B = \begin{pmatrix} 1 & 1 & 2 \\ 6 & 3 & 4 \\ 4 & 2 & 5 \end{pmatrix}, \text{ evaluate}$$

- (i) $5A - 3B$

$$5A = \begin{bmatrix} -20 & 15 & 25 \\ 10 & 30 & -5 \\ 40 & 45 & -30 \end{bmatrix}$$

$$3B = 3 \begin{bmatrix} 1 & 1 & 2 \\ 6 & 3 & 4 \\ 4 & 2 & 5 \end{bmatrix} = \begin{bmatrix} 3 & 3 & 6 \\ 18 & 9 & 12 \\ 12 & 6 & 15 \end{bmatrix}$$

- (ii) BA

$$\begin{bmatrix} -20 & 15 & 25 \\ 10 & 30 & -5 \\ 40 & 45 & -30 \end{bmatrix} \begin{bmatrix} 1 & 1 & 2 \\ 6 & 3 & 4 \\ 4 & 2 & 5 \end{bmatrix} = \begin{bmatrix} -23 & 10 & 19 \\ -8 & 21 & -17 \\ 28 & 39 & 5 \end{bmatrix} \text{ (6 marks)}$$

- Given the matrix

$$M = \begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \\ 2 & 3 & 1 \end{pmatrix}$$

$$\text{Det } M = (1 \times 2 \times 1) + (3 \times 3 \times 3) + (2 \times 2 \times 1) - (3 \times 2 \times 2) - (1 \times 2 \times 3)$$

$$= (33 - 21) = 12$$

Determine its determinant using P.F Sarrus rule.

(4 marks)

- (c) Three currents I_1 , I_2 and I_3 in amperes flowing in a multi-loop circuit satisfy the simultaneous equations.

$$2I_1 - 3I_2 = 13$$

$$-4I_1 + 5I_2 + I_3 = 22$$

$$6I_1 + 8I_2 = 22$$

Use Cramer's rule to solve the equations.

(10 marks)

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